

NASA  
Technical Memorandum 106713

Army Research Laboratory  
Technical Report ARL-TR-306

# Computerized Design of Low-Noise Face-Milled Spiral Bevel Gears

Faydor L. Litvin  
*University of Illinois at Chicago*  
*Chicago, Illinois*

Yi Zhang  
*University of Michigan at Dearborn*  
*Dearborn, Michigan*

and

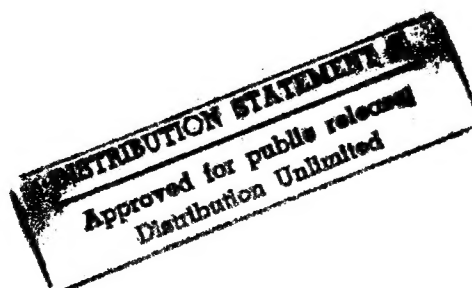
Robert F. Handschuh  
*Vehicle Propulsion Directorate*  
*U.S. Army Research Laboratory*  
*Lewis Research Center*  
*Cleveland, Ohio*



Prepared for the  
23rd Mechanisms Conference  
sponsored by the American Society of Mechanical Engineers  
Minneapolis, Minnesota, September 11-14, 1994



National Aeronautics and  
Space Administration



# Computerized Design of Low-Noise Face-Milled Spiral Bevel Gears

Faydor L. Litvin  
University of Illinois at Chicago  
Chicago, Illinois

Yi Zhang  
University of Michigan at Dearborn  
Dearborn, Michigan

Robert F. Handschuh  
Army Research Laboratory, Vehicle Propulsion Directorate  
NASA Lewis Research Center  
Cleveland, Ohio

19950201 066

## Abstract

An advanced design methodology is proposed for the face-milled spiral bevel gears with modified tooth surface geometry that provides a reduced level of noise and has a stabilized bearing contact. The approach is based on the local synthesis of the gear drive that provides the "best" machine-tool settings. The theoretical aspects of the local synthesis approach are based on the application of a predesigned parabolic function for absorption of undesirable transmission errors caused by misalignment and the direct relations between principal curvatures and directions for mating surfaces. The meshing and contact of the gear drive is synthesized and analyzed by a computer program. The generation of gears with the proposed geometry design can be accomplished by application of existing equipment. A numerical example that illustrates the proposed theory is presented.

## 1. Introduction

Spiral bevel gears have found a broad application in gear transmissions, particularly in high-speed helicopter transmissions. The most important criteria of the quality of meshing of spiral bevel gears applied in high-speed transmissions are low noise and stable bearing contact that must be obtained even under some misalignments.

The analysis of quality of gear drives is based on computerized simulation of meshing and contact of gear drives by Tooth Contact Analysis (TCA) computer programs. The TCA algorithm has been proposed by Litvin and then applied for spiral bevel gears by

Litvin and Go [1]. Commercially developed TCA computer programs for the analysis of meshing of spiral bevel gears and hypoid gears are also available [2, 3, 4]. Later similar programs for hypoid gear drives have been developed as well by Litvin and Gutman [5].

TCA programs are valuable but are designed for the analysis of meshing of gear drives and not for their synthesis. Although the TCA programs enable investigation of the influence of machine-tool setting variation on the quality of meshing and contact, it would be very difficult to determine the "best" machine-tool settings by application of the TCA approach. Litvin and Gutman [5, 6] have developed the method of local synthesis of gear drives. This approach permits the determination of the "best" machine-tool settings considering the conditions of meshing and contact at the mean contact point and within its neighborhood. Usually, the local synthesis approach may provide the set of machine-tool settings, and the role of TCA is to verify the acceptance of the obtained settings, estimate the influence of misalignment and correct (usually slightly) the previously obtained machine-tool settings.

This paper has used both ideas (the local synthesis and TCA approaches) for the design of spiral bevel gears with substantially reduced level of noise and a stabilized bearing contact. These goals have been achieved by application of the following ideas:

Stage 1. The machine-tool settings for the generation of the gear may be considered as given in the local synthesis. The gear machine-tool settings are calculated according to the spiral angle of the gear member determined in the design of blank. The improvement of meshing and contact can be accomplished by the determination of proper machine-tool settings for the pinion only.

It was assumed that the gear is generated by the duplex method (both tooth sides are generated simultaneously) and the pinion tooth sides are generated separately.

Stage 2. The application of local synthesis method is based on the following procedures:

Step 1: The mean contact point  $M$  is chosen on the gear tooth surface. The equations of gear tooth surface  $\Sigma_2$  are known since the gear machine-tool settings have been determined already.

Step 2: The tangency of four surfaces -  $\Sigma_{12}$  (gear generating surface),  $\Sigma_{11}$  (pinion

generating surface),  $\Sigma_2$  (gear surface), and  $\Sigma_1$  (pinion surface) - at the point M is provided.

Step 3: The conditions of meshing and contact of surfaces  $\Sigma_1$  and  $\Sigma_2$  at M are considered, and the following requirements are observed: (i) the gear ratio  $m_{21}(\phi_1) = N_1/N_2$  at M ( $N_1$  and  $N_2$  are the numbers of pinion and gear teeth); (ii) The derivative  $m'_{21}(\phi_1) = \frac{\partial}{\partial \phi_1}[m_{21}(\phi_1)]$  ( $\phi_1$  is the rotation of the pinion) must satisfy the requirement of minimization of transmission errors; (iii) the designated magnitude of the major axis of the instantaneous contact ellipse at M must be observed; and (iv) the designated orientation of the tangent to the contact path at M must be observed as well.

The output of the computerized procedure discussed in Stage 2 are the principal curvatures and directions of the pinion surface at point M.

Stage 3. Surfaces  $\Sigma_{t1}$  and  $\Sigma_1$  of the generating tool and the pinion tooth are considered in contact, and the instantaneous line of contact passes through point M. The principal curvatures and directions at point M of the head-cutter surface  $\Sigma_{t1}$  are determined.

Stage 4. The machine-tool settings of the head-cutter  $\Sigma_{t1}$  with respect to the pinion tooth surface  $\Sigma_1$  are determined.

Stage 5. The equations of pinion tooth surface are derived considering the machine-tool settings of the head-cutter are known with respect to  $\Sigma_1$ .

Stage 6. The TCA program is developed considering the conditions of continuous tangency of tooth surfaces  $\Sigma_1$  and  $\Sigma_2$ . The influence of misalignment of the gear drive on the conditions of meshing and contact can be investigated at this stage.

The following ideas are the theoretical basis of the work in this paper: (i) a predesigned parabolic function of transmission errors can absorb a linear discontinuous function of transmission errors caused by the misalignment of the drive; and (ii) direct relations between the principal directions and curvatures of the two surfaces being in line contact or in point contact can be established.

The theoretical solutions have been tested by computerized simulation of meshing and contact and by direct experimental test of a prototype gear drive. A comparative test for the service life and level of noise has been performed based on a previously existing design and the new design proposed by Litvin and Zhang [9]. The new design reduced the level of noise by 12-18 decibels [11] and the gear drive successfully passed scoring and pitting

Distribution/	
Availability Codes	
Dist	Avail and/or Special
A-1	

test.

The production of spiral bevel gears with the new design can be accomplished using conventional gear grinding equipment but with simpler machine-tool settings as there is no need for the tilt of the head-cutter or the modified roll (variation of motions) in the process of generation. The paper is illustrated with a numerical example.

## 2. Generation Of Pinion And Gear Surfaces

We use the following coordinate systems while considering the process for pinion and gear tooth generation: (i) the fixed one,  $S_{mi}(i = 1, 2)$ , that is rigidly connected to the frame of the cutting machine, and (ii) the movable systems  $S_{ci}$  and  $S_i$  that are rigidly connected to the cradle and the pinion (gear) being generated (Fig. 1). The tool (head-cutter) is mounted on the cradle and coordinate system  $S_{ti}$  of the tool is rigidly connected to the cradle coordinate system  $S_{ci}$ . The pinion (gear) being generated and the cradle perform related rotational motions about axes  $x_i$  and  $z_{mi}$ , respectively. The rotation of the head-cutter about the  $z_{ti}$  axis provides the desired velocity of cutting and is not related to the process of tooth surface generation. The subscripts  $i = 1, 2$  in designations  $S_{mi}$ ,  $S_{ti}$ , and  $S_i$  designate the pinion and the gear, respectively.

The machine-tool settings are represented by the following constant parameters (Fig. 1):  $E_{mi}$  (the blank offset);  $\gamma_{mi}$  (the machine root angle);  $X_{bi}$  (the sliding base);  $X_{pi}$  (the machine center to back);  $S_{ri}$  (the radial setting of the head-cutter);  $r_{ci}$  (the cutter point radius);  $q_i$  (the initial cradle angle);  $\alpha_i$  (the cutter blade angle, Fig. 2);  $R_{ai}$  (the ratio of roll - the ratio of angular velocities of the cradle and the workpiece).

The tool (head-cutter) generating surface (Fig. 2) may be represented in  $S_{ti}$  by the vector function

$$\mathbf{r}_{ti}(s_i, \theta_i) \quad (1)$$

where,  $(s_i, \theta_i)$  are the surface coordinates (the Gaussian coordinates). For the gear, we consider the design parameters of the tools,  $\alpha_2$  and  $r_{c2}$ , and the remaining machine-tool settings as given (they are determined according to the spiral angle of the gear). However,

all the machine-tool settings for the pinion are not known, and they have to be determined by using the procedure of local synthesis.

The generated surface  $\Sigma_i$  can be determined as the envelope to the family of tool surfaces generated in  $S_i$  when the head-cutter and the gear (or pinion) perform the related motions. Surface  $\Sigma_i$  is represented in  $S_i$  in three-parameter form (but with related parameters) by the following equations:

$$\mathbf{r}_i(s_i, \theta_i, \phi_i) = M_{iti}(\phi_i) \mathbf{r}_{ti}(s_i, \theta_i) \quad (2)$$

$$\mathbf{n}_j^{ti} \cdot \mathbf{v}_j^{ti,i} = f(s_i, \theta_i, \phi_i) = 0 \quad (3)$$

Here,  $M_{iti}(\phi_i)$  is the matrix for coordinate transformation;  $\mathbf{n}^{ti}$  and  $\mathbf{v}^{ti,i}$  are the surface unit normal and the relative velocity in generation motion; Subscript  $j$  is equal to  $m_i, t_i, i$  and this designation indicates that vectors of the scalar product in equation (3) can be represented in any of the three coordinate systems mentioned above. Equation (3) is called the equation of meshing [6, 7].

Taking into account that  $s_i$  is a linear parameter in equation (3), it can be easily eliminated and the gear tooth surface can be represented in two-parameter form by the vector function:

$$\mathbf{r}_2(\theta_2, \phi_2) \quad (4)$$

Similarly the pinion tooth surface can be represented, but the parameters of the machine-tool settings are still not determined until the procedure of local synthesis will be accomplished. The mean contact point on surface  $\Sigma_2$  is usually chosen as the mean point of  $\Sigma_2$ .

### 3. Predesign Of Parabolic Function Of Transmission Errors

The transmission function for an ideal gear train is linear and is represented as

$$\phi_2 = \frac{N_1}{N_2} \phi_1 \quad (5)$$

where  $N_i$  is the number of gear teeth,  $\phi_i$  is the rotation angle of the gear. Due to misalignment (change of crossing angle, change of shortest distance between the gear axes, etc.) the transmission function becomes a piecewise almost linear one with the period of transmission errors as the cycle of the meshing of a pair of teeth. Due to the jump of the angular velocity at the junction of cycles, the acceleration approaches to an infinite large value and causes large vibration.

The advanced design of low-noise spiral bevel gears proposed in this paper is based on application of a predesigned parabolic function of transmission errors with a controlled level of the maximal error. It has been shown in [7, 8] that a parabolic function can absorb a linear function and the resulting function of transmission errors will remain parabolic.

The predesigned parabolic function of transmission errors of spiral bevel gears and hypoid gears is provided by certain relationships between the curvatures of the contacting gear tooth surfaces. An alternative option applicable for all types of gears is the possibility to obtain a predesigned parabolic function by application of CNC machines.

#### 4. Direct Relations Between Principal Curvatures And Directions of Contacting Surfaces

Henceforth, we will consider two cases of tangency of contacting surfaces: (i) the surface are in point contact at every instant (when the tangency of the pinion-gear tooth surfaces is discussed), and (ii) when the surfaces are in tangency along a line (when the generation of the pinion and gear tooth surfaces by the head-cutter is discussed).

The derivation of relations between the principal curvatures and directions for two surfaces being in continuous tangency is based on application of the following equations [6, 7]:

$$\mathbf{v}_r^{(2)} = \mathbf{v}_r^{(1)} + \mathbf{v}^{(12)} = \mathbf{v}_r^{(1)} + \mathbf{v}_{tr}^{(1)} - \mathbf{v}_{tr}^{(2)} \quad (6)$$

$$\dot{\mathbf{n}}_r^{(2)} = \dot{\mathbf{n}}_r^{(1)} + \dot{\mathbf{n}}_{tr}^{(1)} - \dot{\mathbf{n}}_{tr}^{(2)} = \dot{\mathbf{n}}_r^{(1)} + (\omega_{tr}^{(1)} - \omega_{tr}^{(2)}) \times \mathbf{n}^{(1)} \quad (7)$$

$$\frac{d}{dt} [\mathbf{n}^{(1)} \cdot \mathbf{v}^{(12)}] = 0 \quad (8)$$

The designation  $\mathbf{v}_r^{(i)}$  and  $\mathbf{v}_{tr}^{(i)}$  designate the linear velocity of a contact point that moves over the surface and with the surface, respectively. The subscripts "r" and "tr" indicate the relative motion and the transfer motion, respectively. The designation  $\dot{\mathbf{n}}_r^{(i)}$  indicates the velocity of the tip of the unit contact normal in relative motion (over the tooth surface), in addition to the velocity of the unit normal in translational motion over the tooth surface. The designation  $\dot{\mathbf{n}}_{tr}^{(i)}$  indicates the velocity of the tip of the unit contact normal in the rotational motion with the tooth surface, that is the transfer motion of the unit normal. Equation (8) is the differentiated equation of meshing.

Figure 3 shows the mean contact point M and the unit vectors along the principal directions ( $\mathbf{e}_s, \mathbf{e}_q$ ) on surface  $\Sigma_2$  and the unit vectors along the principal directions ( $\mathbf{e}_f, \mathbf{e}_h$ ) on surface  $\Sigma_1$ . The above mentioned unit vectors are located in the plane that is tangent to the contacting surfaces at point M. The subscripts 1 and 2 for the contacting surfaces are tentative and may indicate the surfaces of the pinion and the gear, the generated surface and the generating surface.

We may transform the system of equations (6) to (8) taking into account Rodrigues's formula for principal curvatures and reducing the number of scalar equations and unknowns that can be obtained from the above mentioned equations. Finally, we will be able to obtain an overdetermined system of three equations in two unknowns of the following structure [6, 7]:

$$a_{i1}v_s^{(1)} + a_{i2}v_q^{(1)} = a_{i3} \quad (i = 1, 2, 3) \quad (9)$$

Here,

$$v_s^{(1)} = \mathbf{v}_r^{(1)} \cdot \mathbf{e}_s \quad ; \quad v_q^{(1)} = \mathbf{v}_r^{(1)} \cdot \mathbf{e}_q \quad (10)$$

Coefficients  $a_{i1}, a_{i2}$  and  $a_{i3}$  are expressed in terms of parameters of generation motion and principal curvatures  $k_s, k_q, k_f, k_h$  and  $\sigma^{(12)}$ . The consideration of linear equation system (9) yields the following results [6, 7]:



(i) The rank of the augmented matrix of the system is one in the case of line contact of the mating surfaces.

(ii) The rank of the augmented matrix is two in the case of surface point contact.

(iii) In case of line contact we will obtain three equations for the determination of  $k_f, k_h$  and  $\sigma^{(12)}$  in terms of  $k_s, k_q$  and the parameters of motion.

(iv) In case of point contact we will obtain one equation of the following structure:

$$F(k_f, k_h, \sigma^{(12)}, k_s, k_q, m'_{21}) = 0 \quad (11)$$

Two additional equations for the determination of  $k_f, k_h$  and  $\sigma^{(12)}$  may be obtained considering as given the direction of  $\mathbf{v}_r^{(1)}$  (the ratio  $v_s^{(1)}/v_q^{(1)}$ ) and the magnitude of the major axis of the instantaneous contact ellipse.

The system of linear equations (9) must be applied two times: first for the determination, at point M, of the principal curvatures and directions of the pinion (considering the principal curvatures and directions of the gear as known); secondly for the determination of the principal curvatures and directions of the pinion head-cutter (using the obtained principal curvatures and directions of the pinion). Then the "best" machine-tool settings for the pinion generation will be obtained that determines the pinion tooth surface that will be "best" fitted to the gear tooth surface [9].

## 5. Tooth Contact Analysis

The simulation of meshing of pinion and gear tooth surfaces is based on the condition of continuous tangency of the pinion and gear tooth surfaces, and is represented in a fixed coordinate system  $S_h$  (Fig. 4).

Using the condition of continuous tangency, we can obtain five independent nonlinear equations in six unknowns. One of the unknowns is chosen as the input one [4 - 9]. The continuous solution of the system of five nonlinear equations [10] permits the determination of the paths of contact on pinion (gear) tooth surfaces and the transmission errors. In addition, using the relations between the principal curvatures of the contacting surfaces, it becomes possible to determine the dimensions and orientation of the instantaneous contact ellipse and the bearing contact.

## 6. Numerical Example

The numerical example to be shown is the same as the design tested in [11]. The blank data are shown in Table 1 and are the input for two computer programs: (i) for the determination of gear machine-tool settings and (ii) for the local synthesis program. The output for the local synthesis computer program are the pinion machine-tool settings. The gear and pinion machine-tool settings are represented in Tables 2 and 3, respectively. The machine-tool settings are the input for the developed TCA computer programs. The influence of misalignment was simulated by variation of settings V and H (Fig. 4) that represent the offset of the gear drive and the axial displacement of the pinion. The drive offset means that the axes of the rotation of the pinion and the gear are crossed but not intersected, and E is the shortest distance between the crossed axes (Fig. 4). The output of the TCA program are the transmission errors and the bearing contact. Figures 5, 6, and 7 represent the TCA output for the three sets of settings V and H.

The obtained results show that the transmission errors are very low (they do not exceed 8 arc second) and the bearing contact is very stable.

## 7. Conclusion

A methodology for the design of low-noise face-milled spiral bevel gear has been developed. The concept of a predesigned parabolic function of transmission errors that can absorb linear transmission errors caused by manufacturing and assembly has been investigated. Machine tool settings for the spiral bevel gear mesh system are calculated and numerically tested via the tooth contact analysis(TCA) that was developed during this study. From a numerical example, the tolerance of the chosen "best" machine tool settings to misalignment was determined. Misalignments were simulated numerically by displacing the pinion axially and changing the gear offset from their nominal operating locations. The bearing contact remained on the active profile and the transmission error remained the preferred parabolic shape with the same level of error as when the gears operate at their nominal locations.

## Acknowledgment

The authors express their gratitude to Mr. Zachary Henry (Bell Helicopter Co. ), Mr. John Thomas (the Gleason Works), and Mr. David Lewicki (the NASA Lewis Research Center) for their encouragement in this research project and the experimental work for the gear drive with the new design.

**TABLE 1 BLANK DATA(Length in Inch)**

	PINION	GEAR
Number of Teeth	19	62
Pressure Angle		20°
Shaft Angle	95°	
Mean Spiral Angle	35°	
Hand of Spiral	LH	RH
Outer Cone Distance		5.21
Face Width		1.45
Whole Depth	0.30	0.30
Clearance	0.031	0.031
Addendum	0.194	0.075
Dedendum	0.106	0.225
Pitch Angle	17°25'	77°35'
Root Angle	16°34'	75°26'
Face Angle	19°34'	78°26'

**TABLE 2 GEAR MACHINE TOOL SETTINGS**

Blade Angle	20 <sup>0</sup>
Cutter Diameter	7.5
Point Width	0.09
Radial Setting	3.8561
Cradle Angle	52.8084 <sup>0</sup>
Machine Center to Back	0.0
Sliding Base	-0.0333
Ratio of Roll	1.0232
Blank Offset	0.0
Machine Root Angle	75.4333 <sup>0</sup>

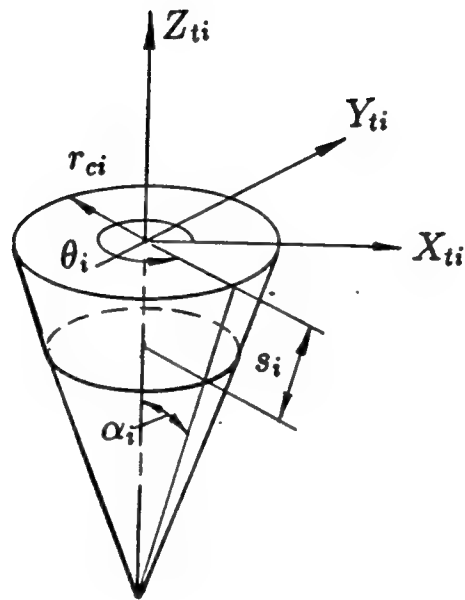
**TABLE 3 PINION MACHINE TOOL SETTINGS**

	Convex	Concave
Cutter Blade Angle	25 <sup>0</sup>	15 <sup>0</sup>
Cutter Point Radius	3.5903	3.9163
Radial Setting	4.1632	3.4909
Cradle Angle	53.4881 <sup>0</sup>	54.3468 <sup>0</sup>
Machine Center to Back	0.038	-0.0489
Sliding Base	-0.0108	0.0139
Ratio of Roll	3.4905	3.1034
Blank Offset	0.4722	-0.5208
Machine Root Angle	16.5667 <sup>0</sup>	16.5667 <sup>0</sup>

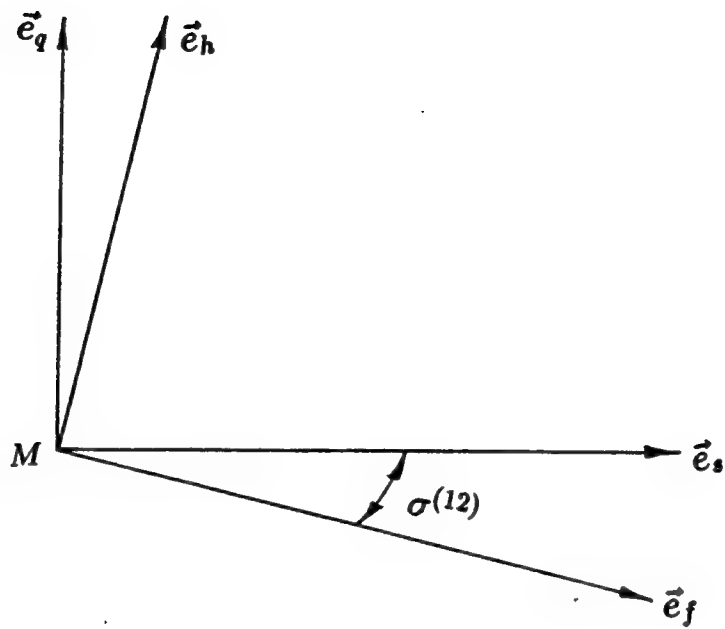
## References

1. Litvin, F. L. and Go, K., 1964, "Improvement of Conditions of Meshing of Spiral Bevel Gears", Proceedings of *Theory of Mechanisms and Machines*, Academy of Sciences of USSR, No. 98- 99.
2. Baxter, M. L., 1973, "Exact Determination of Surfaces for Spiral Bevel Gears", *Industrial Mathematics*, Vol. 23, part 2.
3. Gleason Works, 1981, "Understanding Tooth Contact Analysis", Rochester, NY 14692, Publication No. SD 3139.
4. Wildhaber, E., 1946, "Basic Relationships of Hypoid Gears", *American Machinist*, Vol. 90, No. 4, pp. 108-111.
5. Litvin, F. L. and Gutman, Y., 1981, "Methods of Synthesis and Analysis for Hypoid Gear Drives of Formate and Helixform", *ASME Journal of Mechanical Design*, Vol. 103, pp. 83-113.
6. Litvin, F. L., 1989, "Theory of Gearing", NASA RP-1212, *AVSCOM TR-88-035*.
7. Litvin, F. L., "Gear Geometry and Applied Theory", Prentice Hall, in Press.
8. Litvin, F. L., et al., 1989, "Topology of Modified Helical Gears", *Surface Topology*, Vol. 2, No. 1, pp. 41-59.
9. Litvin, F. L. and Zhang, Y., 1991, "Local Synthesis and Tooth Contact Analysis of Face-Milled Spiral Bevel Gears", NASA CR-4342, *AVSCOM TR-90-C-028*.
10. IMSL MATH/LIBRARY, 1989, "User's Manual", *IMSL(International Mathematics and Statistics Library) Inc.*, Houston.
11. Lewicki, D. L., Handschuh, R. H., Henry, Z. and Litvin, F. L., 1993, "Low-Noise, High-Strength, Spiral-Bevel Gears for Helicopter Transmissions", Proceedings of *29th Joint Propulsion Conference and Exhibit Cosponsored by the AIAA, SAE, ASME, and ASEE*, Monterey, California, June 28-30.





**Fig. 2 TOOL GENERATING SURFACE**



**Fig. 3** PRINCIPAL DIRECTIONS OF CONTACTING SURFACES



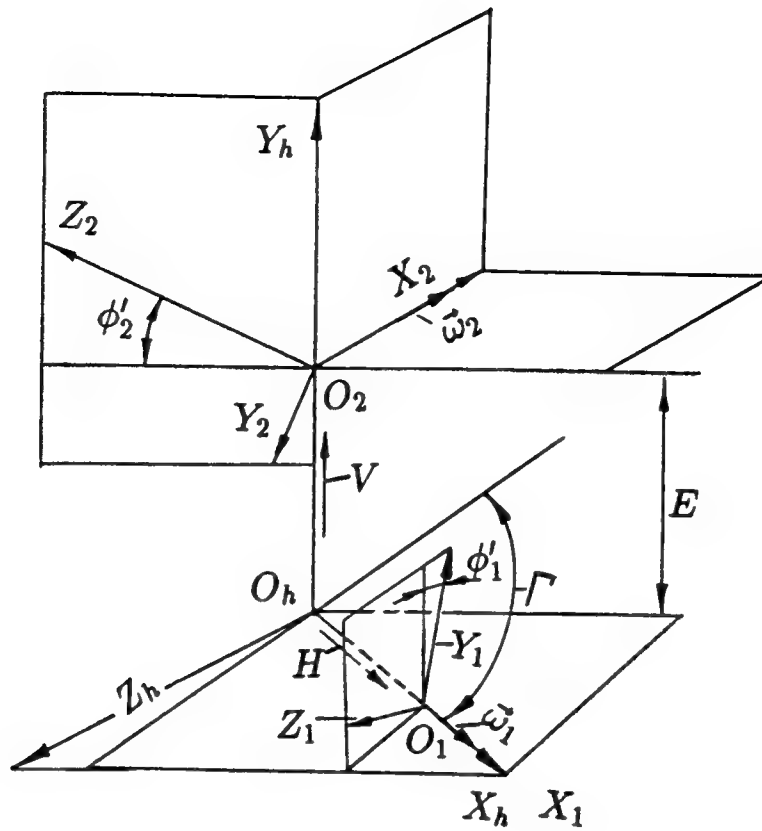
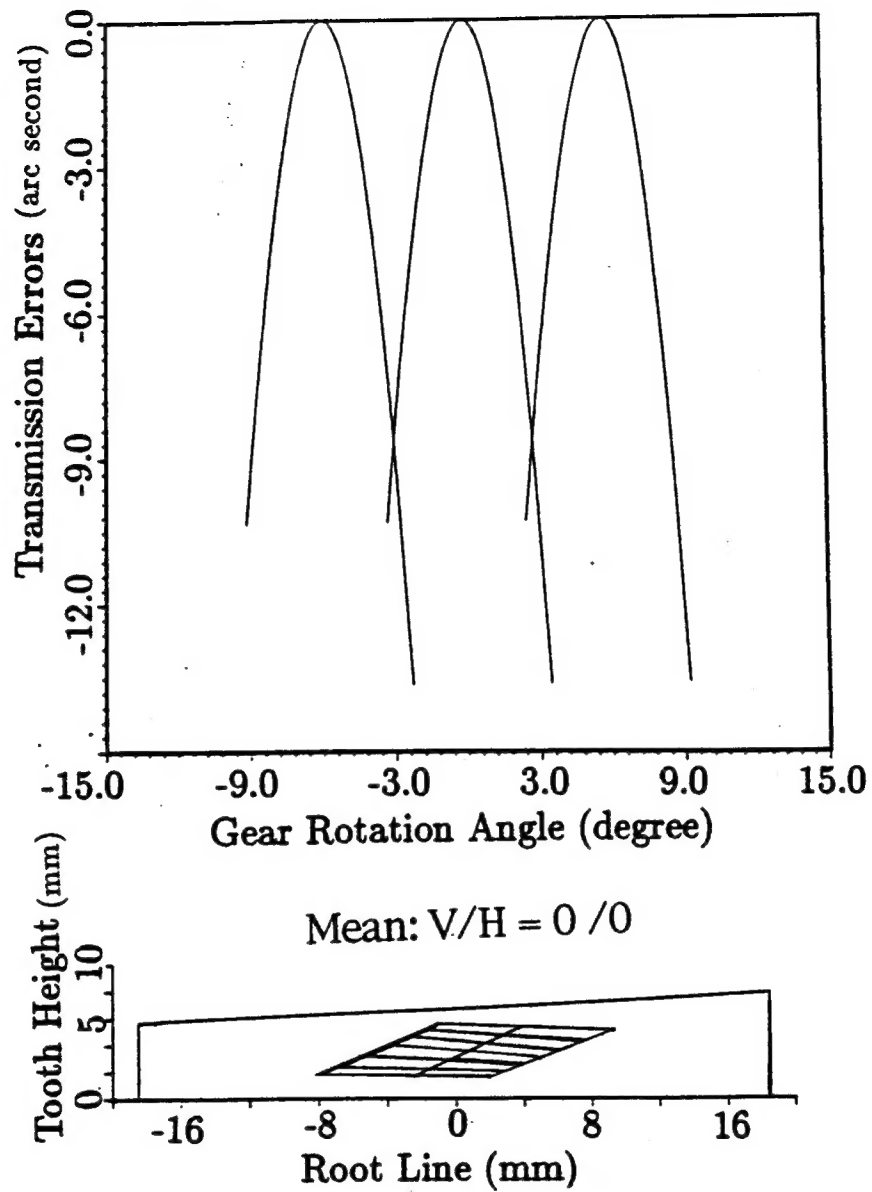
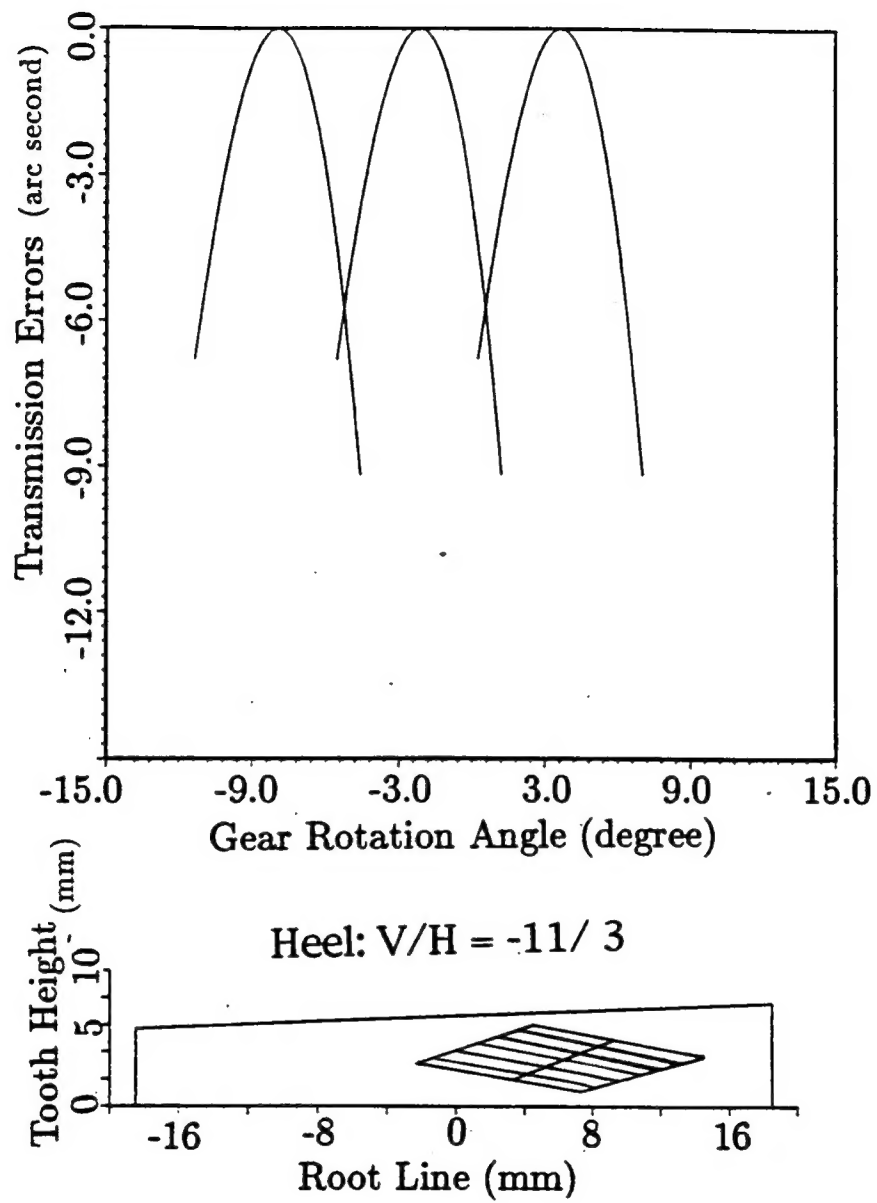


Fig. 4 COORDINATE SYSTEMS FOR TOOTH CONTACT ANALYSIS



**Fig. 5 TRANSMISSION ERRORS AND CONTACT PATTERN  
FOR MEAN POSITION**



**Fig. 6 TRANSMISSION ERRORS AND CONTACT PATTERN  
FOR HEEL POSITION**

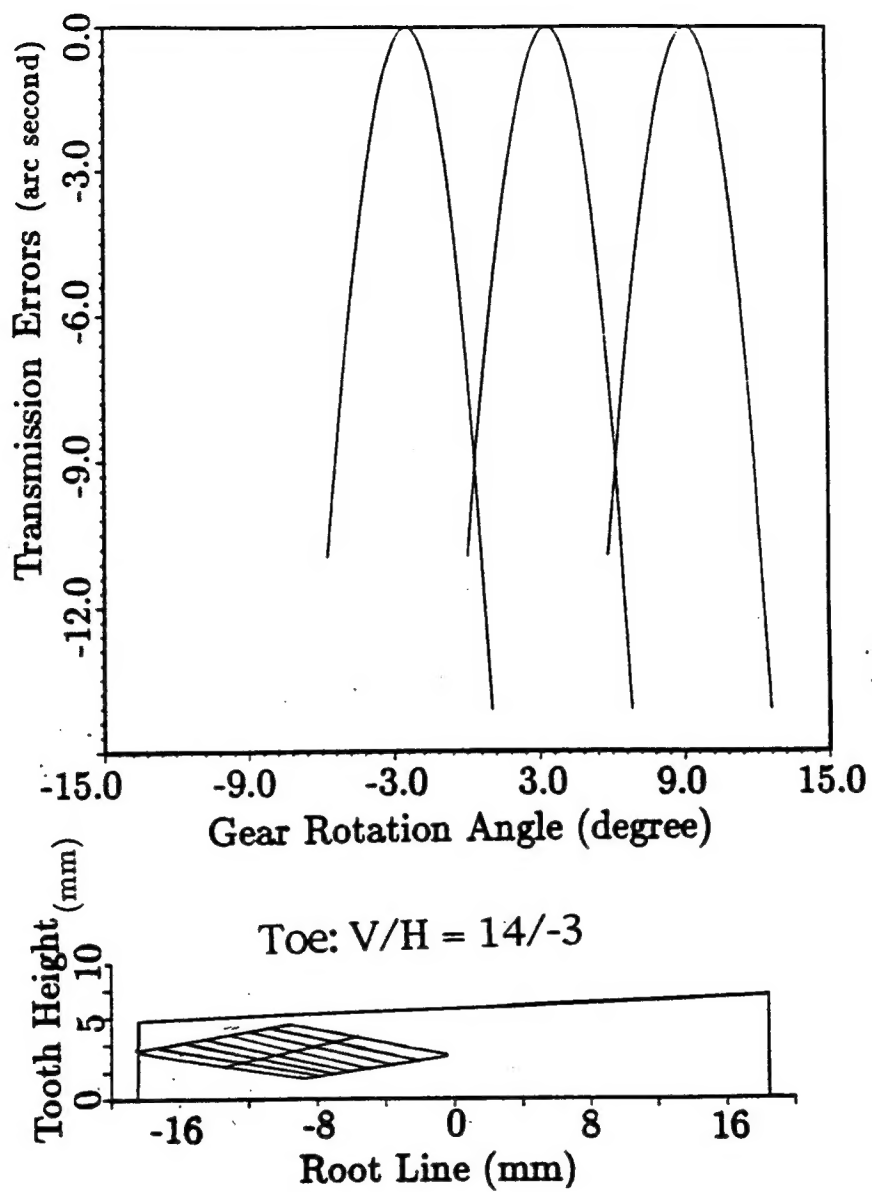


Fig. 7 TRANSMISSION ERRORS AND CONTACT PATTERN  
FOR TOE POSITION

REPORT DOCUMENTATION PAGE			Form Approved OMB No. 0704-0188	
Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503.				
1. AGENCY USE ONLY (Leave blank)	2. REPORT DATE August 1994	3. REPORT TYPE AND DATES COVERED Technical Memorandum		
4. TITLE AND SUBTITLE  Computerized Design of Low-Noise Face-Milled Spiral Bevel Gears		5. FUNDING NUMBERS  WU-505-62-36 1L162211A47A		
6. AUTHOR(S)  Faydor L. Litvin, Yi Zhang, and Robert F. Handschuh				
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) NASA Lewis Research Center Cleveland, Ohio 44135-3191 and Vehicle Propulsion Directorate U.S. Army Research Laboratory Cleveland, Ohio 44135-3191		8. PERFORMING ORGANIZATION REPORT NUMBER  E-9078		
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) National Aeronautics and Space Administration Washington, D.C. 20546-0001 and U.S. Army Research Laboratory Adelphi, Maryland 20783-1145		10. SPONSORING/MONITORING AGENCY REPORT NUMBER  NASA TM-106713 ARL-TR-306		
11. SUPPLEMENTARY NOTES Prepared for the 23rd Mechanisms Conference sponsored by the American Society of Mechanical Engineers, Minneapolis, Minnesota, September 11-14, 1994. Faydor L. Litvin, University of Illinois at Chicago, Chicago, Illinois 60616; Yi Zhang, University of Michigan at Dearborn, Dearborn, Michigan 48823; Robert F. Handschuh, Vehicle Propulsion Directorate, U.S. Army Research Laboratory, NASA Lewis Research Center. Responsible person, Robert F. Handschuh, organization code 2730, (216) 433-3969.				
12a. DISTRIBUTION/AVAILABILITY STATEMENT  Unclassified - Unlimited Subject Category 37		12b. DISTRIBUTION CODE		
13. ABSTRACT (Maximum 200 words)  An advanced design methodology is proposed for the face-milled spiral bevel gears with modified tooth surface geometry that provides a reduced level of noise and has a stabilized bearing contact. The approach is based on the local synthesis of the gear drive that provides the "best" machine-tool settings. The theoretical aspects of the local synthesis approach are based on the application of a predesigned parabolic function for absorption of undesirable transmission errors caused by misalignment and the direct relations between principal curvatures and directions for mating surfaces. The meshing and contact of the gear drive is synthesized and analyzed by a computer program. The generation of gears with the proposed geometry design can be accomplished by application of existing equipment. A numerical example that illustrates the proposed theory is presented.				
14. SUBJECT TERMS  Gears; Gear Teeth; Transmissions			15. NUMBER OF PAGES 21	
			16. PRICE CODE A03	
17. SECURITY CLASSIFICATION OF REPORT Unclassified	18. SECURITY CLASSIFICATION OF THIS PAGE Unclassified	19. SECURITY CLASSIFICATION OF ABSTRACT Unclassified	20. LIMITATION OF ABSTRACT	